

Relic Neutrinos

- Relic Neutrinos in the Standard Model
- Direct Detection?
- Nucleosynthesis
- Beyond the Standard Model

Expectations for the Relic Neutrinos

- $\nu_i, \bar{\nu}_i$ decoupled at $T_D \sim \text{few MeV}$

$$\begin{aligned} f_{\nu_i} &= F_{eq}(p', m_i, \mu_{D_i}, T_D) \\ &= \left[\exp \left(\frac{(p'^2 + m_i^2)^{1/2} - \mu_{D_i}}{T_D} \right) + 1 \right]^{-1} \\ f_{\bar{\nu}_i} &= F_{eq}(p', m_i, -\mu_{D_i}, T_D) \end{aligned}$$

- Subsequently, p' redshifted to $p = p'/\eta$, where $\eta \equiv R(t)/R(t_D)$

$$\begin{aligned}
 f_{\nu_i} &\rightarrow F_{eq}(p', m_i, \mu_{D_i}, T_D) \\
 &= F_{eq}(p, m_i/\eta, \mu_{D_i}/\eta, T_D/\eta) \\
 &= \left[\exp \left(\frac{(p^2 + m_{eff_i}^2)^{1/2} - \mu_i}{T_\nu} \right) + 1 \right]^{-1}
 \end{aligned}$$

$$m_{eff_i} \equiv \frac{m_i}{\eta} \ll m_i, \quad T_\nu \equiv \frac{T_D}{\eta} = \left(\frac{4}{11} \right)^{1/3} T_\gamma \sim 1.9K, \quad \mu_i \equiv \frac{\mu_{D_i}}{\eta}$$

($\mu_i \rightarrow -\mu_i$ for $\bar{\nu}_i$)

- *Form* of relativistic thermal distribution, but (negligible) $m_{eff} \ll T_\nu$
- Actually decoupled and may be non-relativistic

- For $\mu_i = 0$,

$$N_{\nu_i} = N_{\bar{\nu}_i} = \int \frac{d^3p}{e^{p/T_\nu} + 1} \sim 50/cm^3$$

$$\langle p \rangle \sim 3.2T_\nu \sim 5.2 \times 10^{-4} \text{ eV}$$

- For hierarchical pattern

$$m_3 \sim 0.05 \text{ eV}, \quad m_2 \sim 0.005 \text{ eV}, \quad m_1 \ll m_2$$

$$(\langle v_3 \rangle \sim 10^{-2}, \quad \langle v_2 \rangle \sim 10^{-1})$$

- For degenerate pattern, $m_1 \sim m_2 \sim m_3 \lesssim 0.23 \text{ eV}$ (WMAP),

$$\langle v_i \rangle \sim 2 \times 10^{-3} \left(\frac{0.23 \text{ eV}}{m_i} \right)$$

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- Clustering?

$$v_{\text{esc}} \sim 10^{-4} \text{ (Sun)}, \quad 2 \times 10^{-3} \text{ (Galaxy)}, \quad 3 \times 10^{-3} \text{ (Large Cluster)}$$

- Little effect on velocities except degenerate case
- Little clustering unless $m_i \gtrsim 0.3 \text{ eV}$, and then on supercluster scale (Singh, Ma)

- Non-zero asymmetry, $\mu_i \neq 0$:

$$N_{\nu_i} - N_{\bar{\nu}_i} = \frac{T_\nu^3}{6} \left[\xi_i + \frac{\xi_i^3}{\pi^2} \right], \quad \xi_i \equiv \frac{\mu_i}{T_\nu}$$

BBN + CMB: $-0.01 < \xi_e < 0.22$, $|\xi_{\mu,\tau}| < 2.6$

CMB + BBN + equilibration: $|\xi_i| < 0.07$ (Lunardini, Smirnov; Dolgov et al; Wong; Abazajian, Beacom, Bell) (unless new energy source)

But, naive expectation is $|\xi| = O(10^{-11})$

Implications

- Direct Detection
- CMB, large scale structure
 - $\sum_i m_i < 0.71 \text{ eV}$ (small scale suppression)
 - $|\xi_i| < O(2)$ (onset of matter domination)
- BBN
 - Sterile Neutrinos
 - Dirac neutrinos
 - * In Standard Model
 - * With new interactions (Barger, PL, Lee)
 - Hiding new degrees of freedom (Barger, Kneller, PL, Marfatia, Steigman)

Direct Detection

- Incoherent scattering from fixed target

$$\sigma_\nu \sim G_F^2 E_\nu^2 \sim 10^{-62} \text{ cm}^2 (m_\nu = 0), \quad 10^{-58} \text{ cm}^2 (m_\nu \sim 0.1 \text{ eV})$$

- Rate per target atom: $\sigma_\nu j_\nu \sim 10^{-42} (10^{-38})/\text{yr}$ for $j_\nu \sim 3 \times 10^{12}/\text{cm}^2 - \text{s}$
- For $N \sim 10^{21}$ particles in coherence volume of radius $\lambda = 1/p \sim 2.4 \text{ mm} \rightarrow \sigma_\nu j_\nu N^2 \sim 1/\text{yr}$. Signal?
- No practical G_F^2 detection schemes

- Scattering of high energy cosmic ray neutrinos (*Z*-burst) (Weiler)

$$\nu_i \bar{\nu}_i \rightarrow Z \rightarrow \text{particles},$$

at $E^R \sim 4 \times 10^{21} \text{ eV}/m_\nu(\text{eV})$. Secondary nucleons after distance D :

$$E_p \sim \frac{10^{21} \times (0.8)^{D/6 \text{ Mpc}}}{(m_\nu/0.1 \text{ eV})}$$

- Account for $E_p > \text{GZK?}$ (Best fit $m_\nu = 0.26_{-0.14}^{+0.20} \text{ eV}$, Fodor, Katz, Ringwald)
- Future observation? Depends on unknown flux of $\text{UHE}\nu$

Forces, Torques on Macroscopic Objects

- Coherent forward elastic scattering. $\lambda \sim 2.4 \text{ mm} \gg$ atomic spacing suggests ray optics, with refractive indices

$$n_{\nu, \bar{\nu}} - 1 = \frac{2\pi}{p^2} \sum_a N_a f_{\nu, \bar{\nu}}^a(0)$$

$$f_{\nu, \bar{\nu}}^a(0) = \mp \frac{1}{\pi} \frac{G_F E}{\sqrt{2}} K(p, m_\nu) [g_V^a + g_A^a \vec{\sigma}_a \cdot \hat{p}] ,$$

where $K \rightarrow (1, \frac{1}{2})$ for $(m_\nu = 0, p \ll m_\nu)$, and

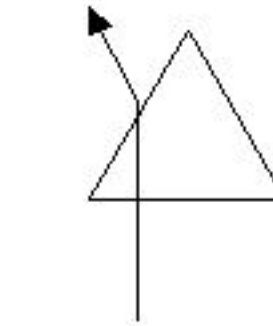
$$-L = \frac{G_F}{\sqrt{2}} \bar{\nu} \gamma_\mu (1 + \gamma_5) \nu \bar{\psi}_a \gamma^\mu (g_V^a + g_A^a \gamma_5) \psi_a$$

For polarized iron and SM couplings,

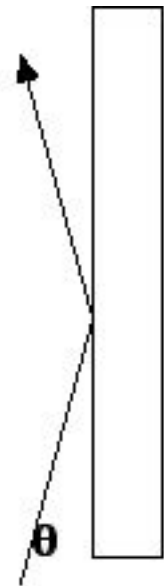
$$n_{\nu_e, \bar{\nu}_e} - 1 = \mp 2.3 \times 10^{-10} [1 + 0.85 \langle \vec{\sigma}_e \rangle \cdot \hat{p}]$$

$$n_{\nu_\mu, \bar{\nu}_\mu} - 1 = \pm 3.1 \times 10^{-10} [1 + 1.2 \langle \vec{\sigma}_e \rangle \cdot \hat{p}]$$

- Net force from refraction for asymmetric geometry?
- Movement through ν sea needed?
- $\nu - \bar{\nu}$ cancellation?



Refraction



Total External Reflection

- Total external reflection (Opher)
 - Net force of $O(G_F)$ for $\theta < \theta_c = \sqrt{2(1-n)} \sim 10 \mu rad$ for $n < 1$ ($\nu_e, \bar{\nu}_\mu, \bar{\nu}_\tau$)
 - No $\nu - \bar{\nu}$ cancellation
 - Need stack of reflectors and motion through ν rest frame
 - Concrete proposal (actually $O(G_F^{3/2})$) (Lewis)

- Effect actually vanishes to $O(G_F, G_F^{3/2})$ (PL, Leveille, Sheiman; Cabibbo, Maiani)
 - Total external reflection only occurs for reflector thickness $>$ skin depth $d \sim \lambda / \sqrt{1 - n} = O(20 \text{ m})$
 - Diffraction at ends unless length $L > 10^7 \text{ m}$

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- $O(G_F^2)$ allowed but too small
- Net torque allowed to $O(G_F)$ for magnetized target (Stodolsky; LSS) but very small
- Other: induced phonons, superconducting currents, etc., small
- Large μ_ν ? (PL, Davoudiasl)

Big Bang Nucleosynthesis

- Parameters

- $\eta = n_B/n_\gamma$ ($\eta_{10} \sim 274 \Omega_b h^2$)
- ΔN_ν (any new source of energy density, relative to one active ν flavor)
- $\xi_e = \mu_{\nu_e}/T$, related to $(N_{\nu_e} - N_{\bar{\nu}_e})/n_\gamma$

- SBBN: $\Delta N_\nu = \xi_e = 0$

- $\nu_e n \leftrightarrow e^- p$ and $e^+ n \leftrightarrow \bar{\nu}_e p$ keep n_n/n_p in equilibrium as long as it is rapid enough

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- Freezeout at $T_\star \sim 1$ MeV, when $\Gamma_{\text{weak}} \sim H$
- $\Gamma_{\text{weak}} = c G_F^2 T^5$
- $H = \left[\frac{8\pi}{3} G_N \rho \right]^{1/2} \sim 1.66 g_\star^{1/2} T^2 / M_{Pl}$
- $g_\star = g_B + \frac{7}{8} g_F$, with $g_F = 10 + 2\Delta N_\nu$
- $T_\star \sim \left(\frac{n_\star^{1/2}}{G_F^2 M_{Pl}} \right)^{1/3}$
- $\frac{n_n}{n_p} = e^{-(m_n - m_p + \mu_{\nu_e})/T_\star} \rightarrow {}^4He$
- 4He mass fraction: $Y_p = \frac{4n_{{}^4He}}{n_H}$ depends strongly on ΔN_ν ($\Delta Y_p \sim 0.013 \Delta N_\nu$) and ξ_e , weakly on η
- $Y_2 = \frac{D}{H}$ depends on η (baryometer)
- Independent determination of η from CMB

- Data

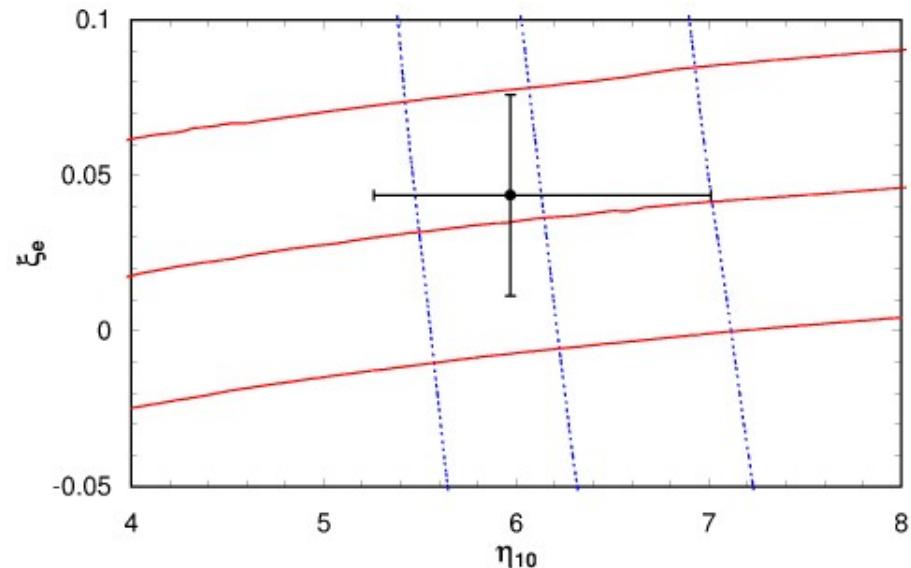
- “High”: $Y_p^{\text{exp}} = 0.244(2)$ (IT)
- “Low”: $Y_p^{\text{exp}} = 0.234(3)$ (OS)
- Will use $Y_P = 0.238 \pm 0.005$
- High D/H not confirmed (hydrogen interloper?) in absorption of background quasars \rightarrow use **Low** $y_D = 10^5(D/H) = 2.6 \pm 0.4$
- $\Omega_b h^2(D/H) = 0.020(2)$
- $\Omega_b h^2(\text{CMB}) \sim 0.0224(9)$ (DASI, BOOMERanG, MAXIMA, WMAP).

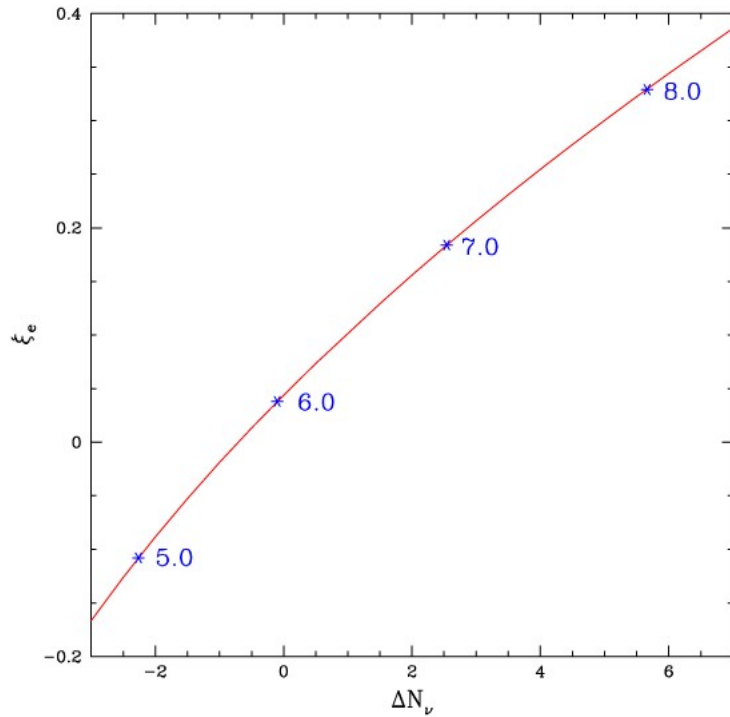
- Nonstandard BBN

- Typical range: $-1.5 < \Delta N_\nu - 16.6\xi_e < 0.3$
- Most contributions to ΔN_ν are positive (**decaying ν_τ** could be negative, but small parameter range)
- Compensations with $\xi_e > 0$ possible (*not* equilibrated $\xi_{\mu,\tau}$)

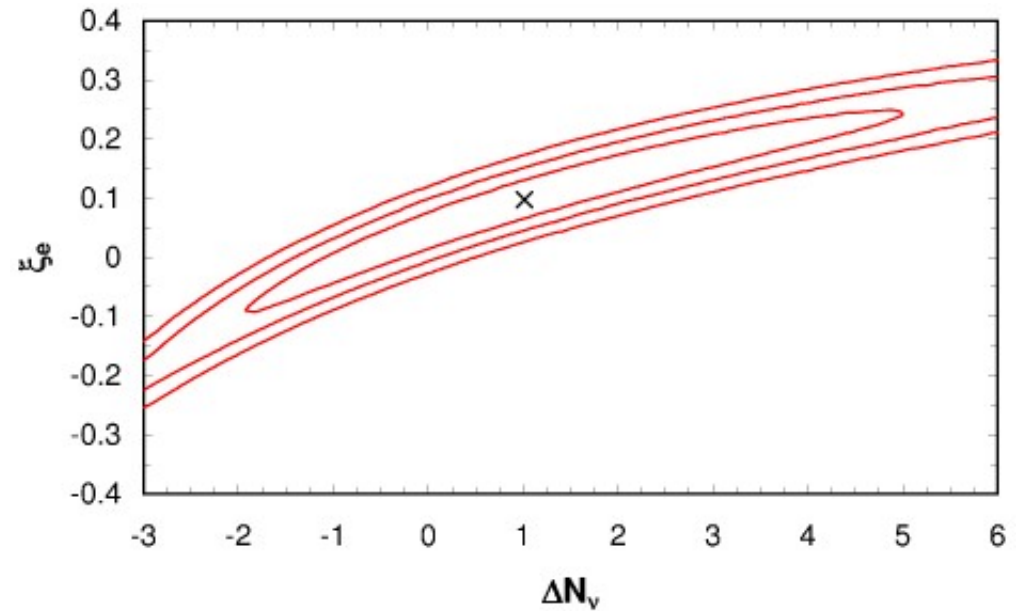
- Best $\Delta N_\nu = 0$ fit for $\xi_e \neq 0$.

- Data point for $y_D = 2.6 \pm 0.4$, $Y_P = 0.238 \pm 0.005$. (Barger, Kneller, PL, Marfatia, Steigman)





Central values of ξ_e as a function of ΔN_ν . The corresponding central values of $10^{10}\eta$ are also shown.



Allowed regions of ξ_e and ΔN_ν from helium and deuterium, including WMAP constraints (Barger, Kneller, PL, Marfatia, Steigman).

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 - New weak interactions: e.g. $f\bar{f} \rightarrow \nu_R \bar{\nu}_R$ by Z' or $Z - Z'$ mixing (Olive, Schramm, Steigman)
 - Results model dependent. Detailed calculations yield large ΔN_ν in E_6 models. (Suppressed in $Z' \nu_R \bar{\nu}_R$ decoupling limit.) (Barger, Lee, PL, PR D67)

- Ordinary-sterile mixing in 4 ν schemes

- Produce ν_s by oscillations and active scattering (decoherence)
 $\rightarrow \Delta N_\nu \sim 1$
- Solar SMA into sterile would have been allowed, but not larger Δm^2 or mixings
- Self-suppression (BFV,SFA): $\Delta L \neq 0 \Rightarrow$ could self-generate lepton asymmetries to either (a) suppress sterile production or (b) generate compensating ξ_e

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- Self-suppression now excluded for all 3+1 and 2+2 parameters (Di Bari, PR D65). (Also, solar + atm. fits (Maltoni et al, NP B643)).
- Could save with large ($O(1)$) preexisting asymmetry or 5th (heavier) sterile ν_s leading to asymmetry

The GUT Seesaw

- Elegant mechanism for small Majorana masses
- Leptogenesis
- Expect small mixings in simplest versions (can evade by lopsided e/d , Majorana textures, etc.)
- Large Majorana often forbidden, e.g., by extra $U(1)$'s
- Direct Majorana masses and large scales forbidden in some string constructions
- GUTs, adjoint Higgs, large Higgs hard to accomodate in simplest heterotic constructions

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 - Small Majorana from loops, R_p violation, or TeV seesaw
 - Small Dirac from large extra dimension or by higher dimensional operators in intermediate scale models (e.g. $U(1)'$)

$$L_\nu \sim \left(\frac{S}{M_{Pl}} \right)^p L N_L^c H_2, \quad \langle S \rangle \ll M_{Pl}$$

$$\Rightarrow m_\nu \sim \left(\frac{\langle S \rangle}{M_{Pl}} \right)^p \langle H_2 \rangle$$

(flexible seesaw alternative; can also yield large ordinary-sterile mixing (PL))

A TeV scale Z' ?

- Motivations

- Strings, GUTs, DSB often involve extra $U(1)'$ (GUTs require extra fine tuning for $M_{Z'} \ll M_{\text{GUT}}$)
- String models: radiative breaking of electroweak (SUGRA or gauge mediated) often yield ew/TeV scale Z' (unless breaking along flat direction \rightarrow intermediate scale)
- Solution to μ problem

$$W \sim h S H_u H_d,$$

S = standard model singlet, charged under $U(1)'$. $\langle S \rangle$ breaks $U(1)'$, $\mu_{eff} = h \langle S \rangle$ (like NMSSM, but no domain walls)

- Experimental limits (precision and collider) model dependent, but typically $M_{Z'} > (500 - 800) \text{ GeV}$ and $Z - Z'$ mixing $|\delta| < \text{few} \times 10^{-3}$
- Models: $M_{Z'} \gtrsim 10M_Z$ by either modest tuning (Demir et al), or by secluded sector (Erlar, PL, Li)
- Implications
 - Exotics
 - FCNC (especially in string models)
 - Non-standard Higgs masses, couplings (doublet-singlet mixing)
 - Non-standard sparticle spectrum
 - Enhanced possibility of EW baryogenesis (Han, Kang, PL, Li)

Big Bang Nucleosynthesis Constraints on Z'

(Barger, Lee, PL, PR D67, 2003)

- Suppose $U(1)'$ forbids large Majorana mass for ν_R needed for traditional seesaw \Rightarrow need TeV seesaw or small Dirac masses
- $\nu_L \bar{\nu}_L, e^+ e^- \rightarrow Z' \rightarrow \nu_R \bar{\nu}_R$ (or $W' \rightarrow e \nu_R$, etc) can produce ν_R efficiently prior to BBN (Olive, Schramm, Steigman, 1979)

- Rough estimate: $\sigma_{Z'}/\sigma_Z \sim (M_Z/M_{Z'})^4$
- ν_R decouples for reaction rate $\Gamma_{Z'}(T) = n\langle\sigma_{Z'}v\rangle \sim G_W^2(M_Z/M_{Z'})^4 T^5$ comparable to expansion rate $H \sim T^2/M_{Pl}$ at,

$$T_d(\nu_R) \sim \left(\frac{M_{Z'}}{M_Z}\right)^{4/3} T_d(\nu_L),$$

where $T_d(\nu_L) \sim \text{few } MeV$.

- ν_R subsequently diluted by annihilations of heavy particles (c, τ, s, μ, π) and by the confinement of quarks and gluons at quark-hadron transition at $T_c \sim 150 - 400 \text{ MeV}$ (these reheat e^\pm, ν_L, γ but not ν_R)

- Full treatment requires detailed contributions of heavy particles to interactions, expansion rate, and entropy; and $Z - Z'$ mixing
 - For three types of right-handed neutrinos

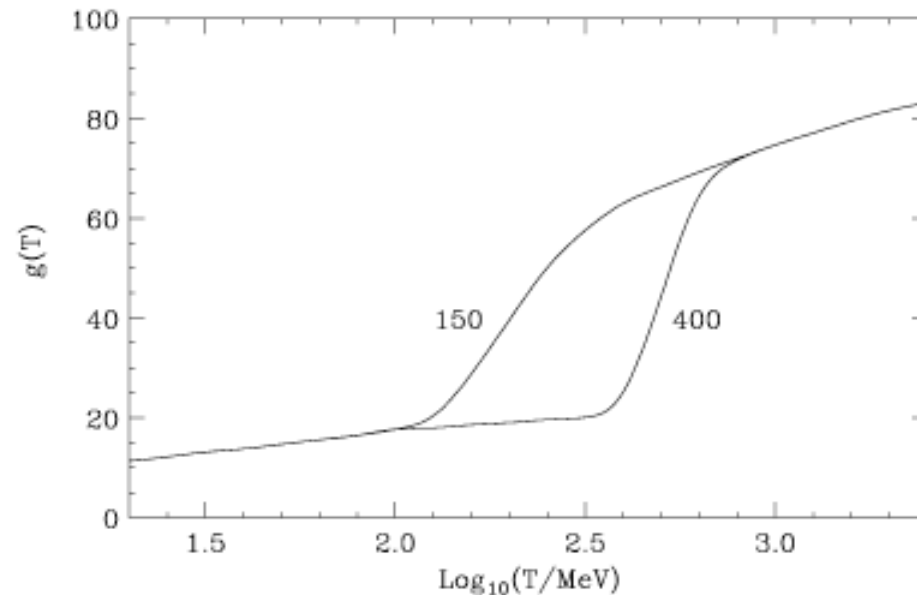
$$\Delta N_\nu = 3 \cdot \left(\frac{T_{\nu_R}}{T_{BBN}} \right)^4 = 3 \left(\frac{g(T_{BBN})}{g(T_d(\nu_R))} \right)^{4/3},$$

Follows from entropy conservation.

$T_d(\nu_R)$ is the ν_R decoupling temperature, $g(T) \sim g_B(T) + \frac{7}{8}g_F(T)$ (+ mass effects), $g_{B,F}(T)$ are the number of bosonic and fermionic relativistic degrees of freedom in equilibrium at temperature T .

- $g(T_{BBN}) = 43/4$ from the three active neutrinos, e^\pm , and γ , and $g(T)$ increases (in this approximation) as a series of step functions at higher temperature. Above quark-hadron temperature $T_c \sim 150 - 400 \text{ MeV}$ include quarks and gluons (u, d, s, \dots); below T_c may have pions.

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$g(T)$ for $T_c = 150$ and 400 MeV , not including the three ν_R (Olive et al.)

- Find $T_d(\nu_R)$ by comparing $\overline{\nu_R}\nu_R$ annihilation rate

$$\Gamma(T) = \sum_i \Gamma_i(T) = \sum_i \frac{n_{\nu_R}}{g_{\nu_R}} \langle \sigma v(\overline{\nu_R}\nu_R \rightarrow \overline{f_i}f_i, \pi^+\pi^-) \rangle,$$

with expansion rate

$$H(T) = \sqrt{\frac{8\pi G_N \rho(T)}{3}} = \sqrt{\frac{4\pi^3 G_N g'(T)}{45}} T^2,$$

with $g'(T) = g(T) + \frac{21}{4}$, for the 3 ν_R .

– For $\sigma_i(s) \equiv \sigma(\overline{\nu_R}\nu_R \rightarrow \overline{f_i}f_i)$

$$\begin{aligned}\sigma_i(s) = & N_C^i \frac{s\beta_i}{16\pi} \left\{ \left(1 + \frac{\beta_i^2}{3}\right) ((G_{RL}^i)^2 + (G_{RR}^i)^2) \right. \\ & \left. + 2(1 - \beta_i^2) G_{RL}^i G_{RR}^i \right\}\end{aligned}$$

where (for $s \ll M_{Z_1}^2, M_{Z_2}^2$)

$$\begin{aligned}G_{RX}^i = & g_Z'^2 Q(\nu_R) Q(f_{iX}) \left(\frac{\sin^2 \delta}{M_{Z_1}^2} + \frac{\cos^2 \delta}{M_{Z_2}^2} \right) \\ & - g_Z' g_Z Q(\nu_R) Q_Z(f_{iX}) \left(\frac{\sin \delta \cos \delta}{M_{Z_1}^2} - \frac{\sin \delta \cos \delta}{M_{Z_2}^2} \right),\end{aligned}$$

$Q(Q_Z) = Z'(Z)$ charge, $X = L$ or R , $\beta_i \equiv \sqrt{1 - 4m_{f_i}^2/s}$, N_C^i is the color factor of f_i , and $\delta = Z - Z'$ mixing angle.

The E_6 $U(1)'$ Model

- Standard anomaly-free $U(1)'$ model, but not full GUT (proton decay)
- Two $U(1)'$ factors

$$E_6 \rightarrow SO(10) \times U(1)_\psi \rightarrow SU(5) \times U(1)_\chi \times U(1)_\psi$$

Assume one light, with charge

$$Q = Q_\chi \cos \theta_{E6} + Q_\psi \sin \theta_{E6}$$

Special case, $U(1)_\eta$: $\theta_{E6} = 2\pi - \tan^{-1} \sqrt{\frac{5}{3}} = 1.71\pi$.

The (family-universal) charges of the $U(1)_\chi$ and the $U(1)_\psi$.

Fields	Q_χ	Q_ψ
u_L	$-1/2\sqrt{10}$	$1/2\sqrt{6}$
u_R	$1/2\sqrt{10}$	$-1/2\sqrt{6}$
d_L	$-1/2\sqrt{10}$	$1/2\sqrt{6}$
d_R	$-3/2\sqrt{10}$	$-1/2\sqrt{6}$
e_L	$3/2\sqrt{10}$	$1/2\sqrt{6}$
e_R	$1/2\sqrt{10}$	$-1/2\sqrt{6}$
ν_L	$3/2\sqrt{10}$	$1/2\sqrt{6}$
ν_R	$5/2\sqrt{10}$	$-1/2\sqrt{6}$

- $Z - Z'$ mixing δ

(A0) $\delta = 0$ (no mixing)

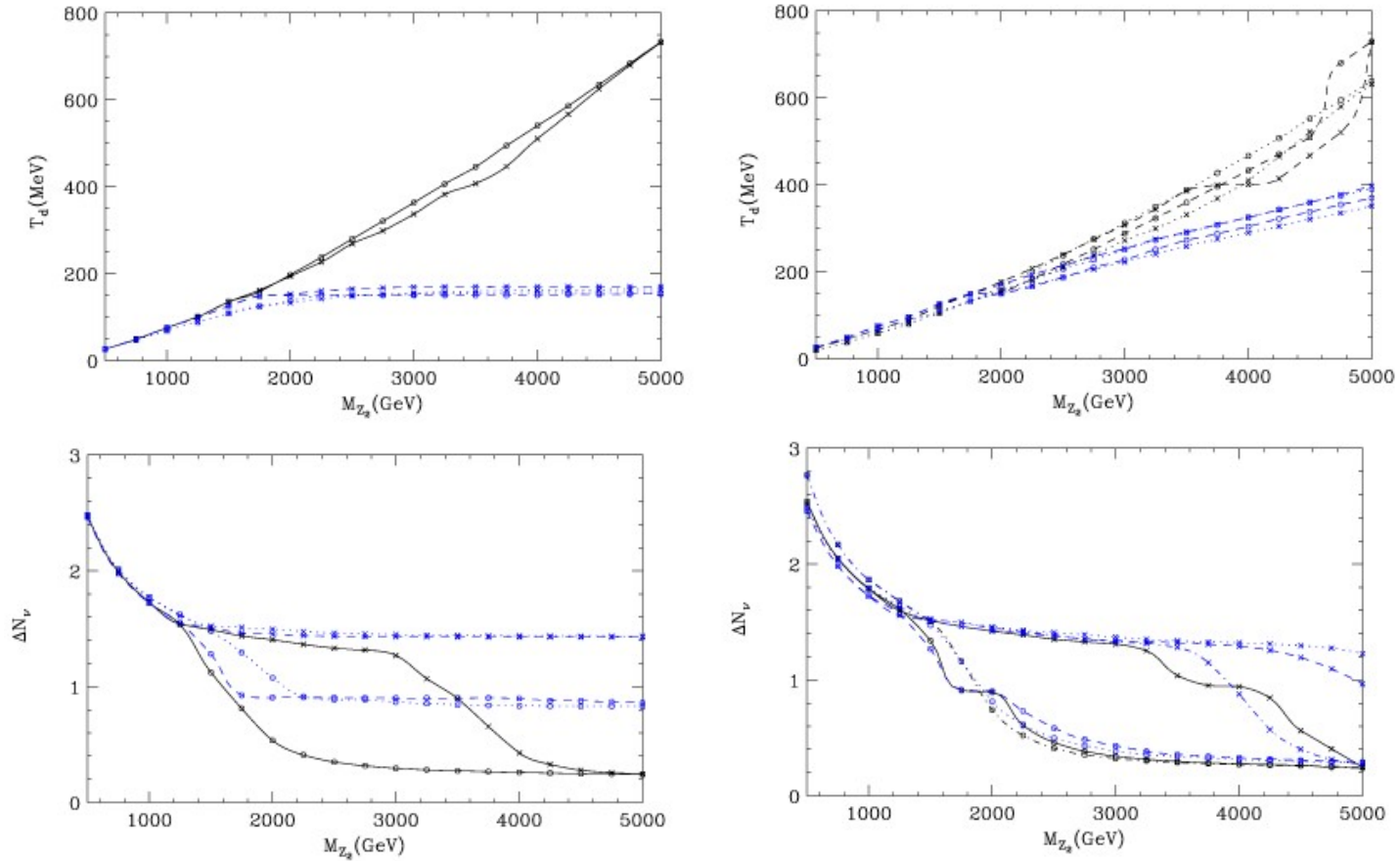
(A1) $|\delta| < 0.0051/M_{Z_2}^2$ (mass – mixing relation for 27 – plet)

(A2) $|\delta| < 0.0029/M_{Z_2}$ (ρ_0 constraint)

(A3) $|\delta| = 0.002$ (maximal mixing allowed for $M_{Z_2} \sim 1 \text{ TeV}$).

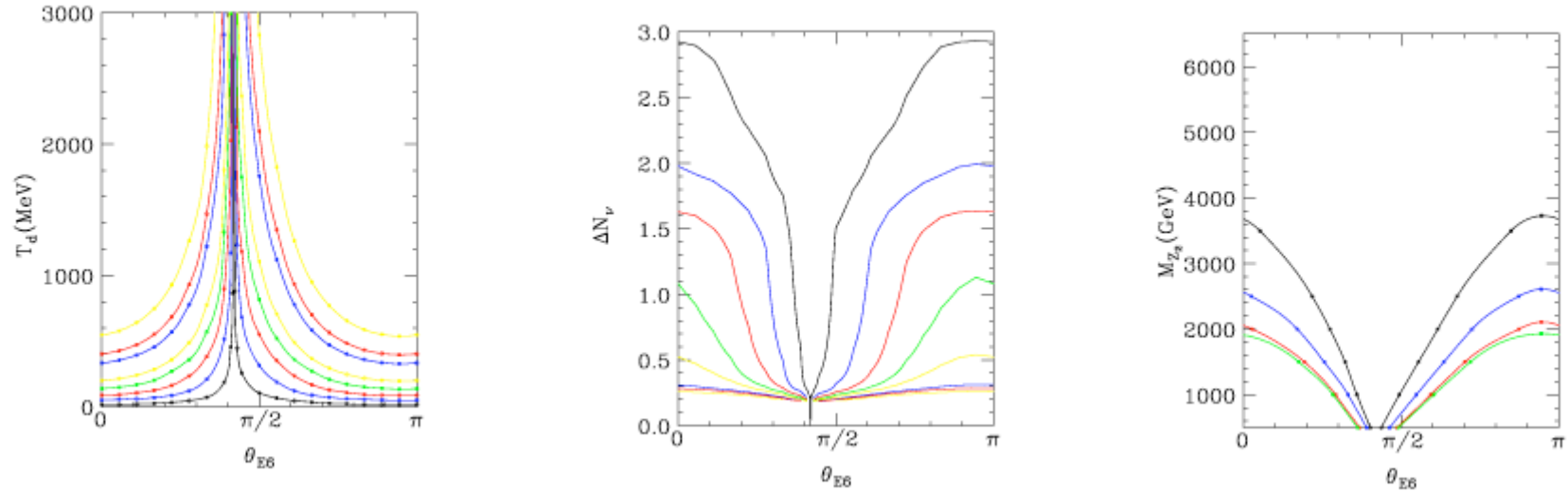
(A1 more stringent than A2 and A3 in the large mass range)

Results for the η Model



T_d (top) and ΔN_ν (bottom) for the η model, for $T_c = 150$ MeV (circles) and 400 MeV (crosses). Left: A0 and A3. Right: A1 and A2.

Results for the General E_6 Model



T_d (left) and ΔN_ν (middle) for $M_{Z_2} = 500, 1000, 1500, 2000, 2500, 3500, 4000$, and 5000 GeV, for $T_c = 150$ MeV and no mixing. Larger M_{Z_2} corresponds to higher T_d and smaller ΔN_ν . Right: M_{Z_2} corresponding to $\Delta N_\nu = 0.3, 0.5, 1.0$ and 1.2, with larger ΔN_ν corresponding to smaller M_{Z_2} . χ , ψ , and $-\eta$ correspond to $\theta_{E6} = 0, \pi/2, 0.71\pi$. The results including mixing are similar.

- Very sensitive to θ_{E6} , δ , and T_c
- η model
 - $\Delta N_\nu < 0.3 \Rightarrow M_{Z'} > (2.5 - 3.2) \text{ TeV}$ for $T_c = 150 \text{ MeV}$
 - $\Delta N_\nu < 0.3 \Rightarrow M_{Z'} > (4.0 - 4.9) \text{ TeV}$ for $T_c = 400 \text{ MeV}$
- General E_6 case (all mixing assumptions)
 - $\Delta N_\nu < 0.3$ for all θ_{E6} for $M_{Z'} > 2.4 \text{ TeV}$ ($T_c = 150 \text{ MeV}$)
(more stringent for $T_c = 400 \text{ MeV}$)
 - Limits disappear near ν_R decoupling angle $\theta_{E6} = 0.42\pi$ ($\chi = 0$, $\psi = \pi/2$, $-\eta = 0.71\pi$)
- Constraints often much more stringent than current direct/indirect; comparable to LHC range
- For $\Delta N_\nu < 0.3$, somewhat more stringent than supernova limits, but different uncertainties.

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- Ways out
 - TeV seesaw or other non-Dirac mechanism
 - Large ξ_e asymmetry (equilibration limits don't apply because of ΔN_ν)
 - ν_R decoupling from Z' (can occur naturally in $U(1)' \times U(1)'$ model)

Natural ν_R Decoupling in $U(1)' \times U(1)'$

- Break $U(1)' \times U(1)'$ by standard model singlets $\tilde{\nu}_R + \tilde{\nu}_R^*$ and $\tilde{s}_L + \tilde{s}_L^*$ from 27, 27*-plets. D terms:

$$\begin{aligned} V_\chi + V_\psi &= \frac{g'^2}{2} \left[\frac{5}{2\sqrt{10}} (|\tilde{\nu}_R|^2 - |\tilde{\nu}_R^*|^2) \right]^2 \\ &+ \frac{g'^2}{2} \left[\frac{1}{\sqrt{24}} (-|\tilde{\nu}_R|^2 + |\tilde{\nu}_R^*|^2 - 4|\tilde{s}_L|^2 + 4|\tilde{s}_L^*|^2) \right]^2, \end{aligned}$$

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 \end{aligned}$$

- D -flat for $|\tilde{\nu}_R|^2 = |\tilde{\nu}_R^*|^2 \equiv |\tilde{\nu}|^2$ and $|\tilde{s}_L|^2 = |\tilde{s}_L^*|^2 \equiv |\tilde{s}|^2$. May also be F -flat, broken by soft masses,

$$V(\tilde{\nu}, \tilde{s}) = m_{\tilde{\nu}}^2 |\tilde{\nu}|^2 + m_{\tilde{s}}^2 |\tilde{s}|^2$$

- Z' mass terms

$$\begin{aligned}\mathcal{L} = & g'^2 \left(-\frac{5}{2\sqrt{10}} Z_\chi + \frac{1}{\sqrt{24}} Z_\psi \right)^2 (|\tilde{\nu}_R|^2 + |\tilde{\nu}_R^*|^2) \\ & + g'^2 \left(\frac{4}{\sqrt{24}} Z_\psi \right)^2 (|\tilde{s}_L|^2 + |\tilde{s}_L^*|^2)\end{aligned}$$

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For $m_{\tilde{s}}^2 > 0$ and $m_{\tilde{\nu}}^2 < 0$ the breaking will occur along $|\tilde{\nu}_R| = |\tilde{\nu}_R^*|$ very large, with the potential ultimately stabilized by loop corrections or higher dimensional operators. \tilde{s}_L and \tilde{s}_L^* will acquire (usually different) TeV-scale expectation values.

- $Z_1 \equiv \frac{1}{\sqrt{24}}Z_\chi + \frac{5}{2\sqrt{10}}Z_\psi$ **at TeV scale** (Z_1 decouples from ν_R , avoiding BBN, supernova constraints)
- $Z_2 \equiv -\frac{5}{2\sqrt{10}}Z_\chi + \frac{1}{\sqrt{24}}Z_\psi$ **superheavy** (can use Z_2 scale for small Dirac ν_R mass by HDO)

Conclusions

- Relic neutrinos important for BBN, CMB, structure, ν mass spectrum
- Direct detection extremely difficult. Z burst?
- Z' very well motivated, but may forbid canonical large-scale seesaw
- Light Dirac (e.g., by HDO) produced efficiently by Z'
 - Strong BBN constraints
 - Relax by ξ_e asymmetry or ν_R decoupling